

Recap + CH 2: Kinematics in one Dimension Febrero 4, 2019

\* Complete motion diagram → label velocity vectors  
 → show acceleration vector anytime  $\vec{a}$  changes

⇒ Prefixes

⇒ Converting units → multiply by conversion factors  
 (ratios of units that equal one) +  
 Cancel units algebraically. END

Physics 4A lectures are 75 minutes?  
 How many microcenturies is this?

$$75 \text{ min} = \frac{75 \text{ min}}{60 \text{ min}} \cdot \frac{1 \text{ hr}}{24 \text{ hrs}} \cdot \frac{1 \text{ day}}{365.25 \text{ days}} \cdot \frac{1 \text{ yr}}{100 \text{ yrs}} \cdot \frac{1 \text{ century}}{100 \text{ yrs}}$$

$$\frac{1 \text{ century}}{10^{-6} \text{ century}} = \frac{1.426 \mu \text{ centuries}}{1.4 \mu \text{ centuries}}$$

$$15.5 \text{ km}^2 = \frac{15.5 \text{ km}^2}{(1 \text{ km})^2} \cdot \left( \frac{10^3 \text{ m}}{1 \text{ km}} \right)^2 = 15.5 \times 10^6 \text{ m}^2 = 1.55 \times 10^7 \text{ m}^2$$

Ex Show  $1 \text{ g/cm}^3 = 10^{-3} \text{ kg/m}^3$

Chapter 2: Kinematics in One Dimension

Quick Calculus Review

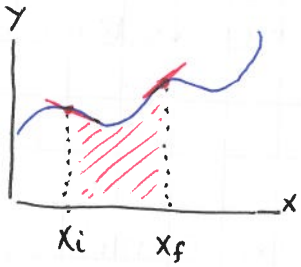
$y(x) \rightarrow y$  is a function of  $x$

Ex  $y(x) = 4x^2 - 3x$   
 $y(x) = 12x^3 - 4x^2 + 7 = 36x^2 - 8x$

cha

February 9, 2019

what does  $dy/dx$  represent?  $\rightarrow$  Slope of the Curve of  $y$  vs.  $x$



what does  $\int_{x_i}^{x_f} y(x) dx$  represent?

$\downarrow$   
area under the curve between  $x_i$  and  $x_f$

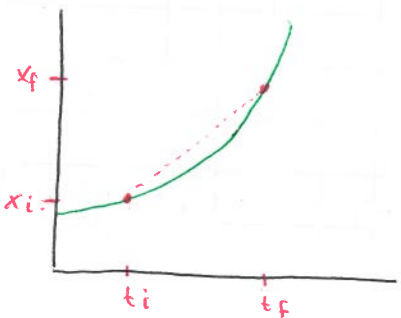
**POSITION VS. TIME + UNIFORM MOTION**

Preview: graph of position vs. time  $\rightarrow$  Slope of position-vs-time gives velocity  
 $\rightarrow$  area under position-vs-time gives nothing useful

graph of velocity-vs-time  $\rightarrow$  Slope of velocity-vs-time gives acceleration  
 $\rightarrow$  area under velocity-vs-time gives  $\Delta$  displacement

graph of acceleration-vs-time  $\rightarrow$  Slope of acceleration-vs-time give us nothing useful (jerk)  
 $\rightarrow$  Area under acceleration-vs-time give us  $\Delta$  velocity ( $\Delta \vec{v}$ )

$x(t)$  } Position (x or y) as a function of time  
 $y(t)$  }



Slope of line connecting two points:

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{x_f - x_i}{t_f - t_i} = \frac{\Delta x}{\Delta t} = \text{avg. vel. during the time interval } \Delta t$$

ch 2

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\* Slope of tangent line  $v_x = dx/dt =$  Slope of position vs time graph at time  $t$

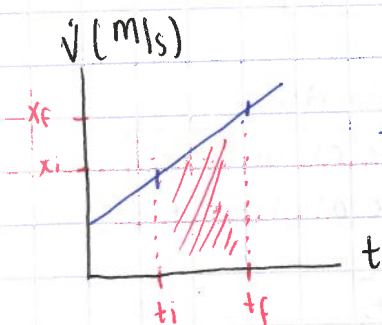
### Velocity-vs-time graphs

$a = dv/dt \rightarrow$  acceleration is the slope of the tangent line of velocity-vs-time.

$V = \frac{dx}{dt} \rightarrow$  Instantaneous velocity  $v = dx/dt =$  Slope of tangent line of position-vs- $t$

$$V = dx/dt \quad \rightarrow \quad \int_{t_i}^{t_f} v dt = \int_{x_i}^{x_f} dx \quad \rightarrow \quad x \Big|_{x_i}^{x_f} = (x_f - x_i) = \Delta x$$

$\hookrightarrow$  area under curve of velocity-vs-time between  $t_i$  and  $t_f$

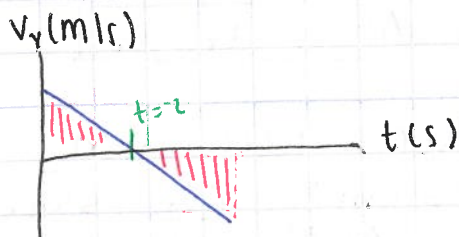


\* Area under curve  $\leftarrow$  between  $t_i$  to  $t_f$  gives the displacement during time interval  $(\Delta t)$

\* To get  $x_f$ , we need to be given  $x_i$

$\hookrightarrow$  Area under curve only give us  $\Delta x$

\* Area under curve gives the displacement but not the distance traveled.



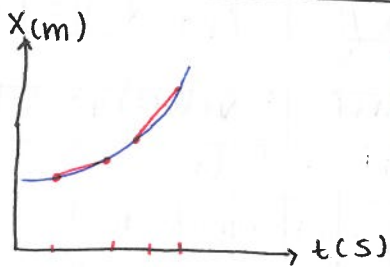
RECAP

→ Converting Units

Chapter 2

quick review of calculus → what is  $\frac{dy}{dx}$   
 → what is  $\int_{x_i}^{x_f} y(x) dx$

Position - vs - time graphs



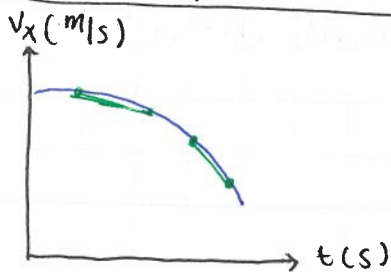
$$v_{avg, x} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i}$$

instantaneous velocity

$$v_x = \frac{dx}{dt} = \text{slope of tangent line at time } t$$

$$= \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

Velocity - Versus - time graph



$$a_{avg, x} = \frac{\Delta v_x}{\Delta t} = \frac{v_{xf} - v_{xi}}{t_f - t_i}$$

Instantaneous acceleration

$$a_x = \frac{dv_x}{dt} = \lim_{\Delta t \rightarrow 0} \frac{\Delta v_x}{\Delta t} = \text{slope of tangent line at time } t$$

• area under curve of velocity - vs - time graph gives displacement  $\Delta x = x_f - x_i$

CH2

February 5, 2019

$$V = \frac{dx}{dt}$$

$$\int_{t_i}^{t_f} v dt = \int_{t_i}^{t_f} dx/dt dt$$

Area under velocity - vs - time

Curve between  $t_i$  +  $t_f$

$$\int_{t_i}^{t_f} \frac{dx}{dt} dt \rightarrow x(t) \Big|_{t_i}^{t_f} = x_f - x_i = \Delta x$$

**Problem 2.11**

for velocity - vs - time graph:

- $x_f = x_i + \text{area under curve of } v \text{ vs } t$
- $v_x \rightarrow$  Read right from graph
- $a_x = dv_x/dt \rightarrow$  find slope of curve

a) each square has area of  $(2\text{m/s})(1\text{s}) = 2\text{m}$   
between  $0 + 2\text{s} \rightarrow 4$  squares

$$\Delta x = 4 \times 2\text{m} = 8\text{m}$$

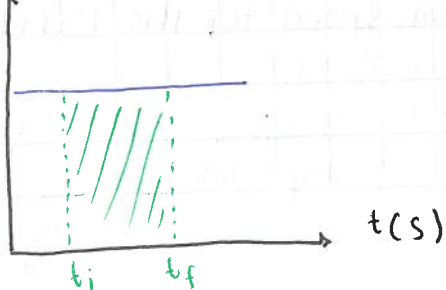
$$x_f = x_i + \Delta x = 2.0\text{m} + 8.0\text{m} = 10.0\text{m}$$

b)  $v_x = 2\text{m/s}$  at  $t = 2.0\text{s}$

c) Slope =  $\frac{(0\text{m/s} - 6\text{m/s})}{(3\text{s} - 0\text{s})} = -2\text{m/s}^2$

**Acceleration - vs - time graphs**

$a(\text{m/s}^2)$



$$a_x = dv_x/dt$$

$$\int_{t_i}^{t_f} a_x dt = \int_{t_i}^{t_f} \frac{dv_x}{dt} dt = v_x(t) \Big|_{t_i}^{t_f} = \Delta v_x = v_{x_f} - v_{x_i}$$

area under acceleration - vs - time curve between  $t_i$  +  $t_f$

\* Area under curve of acceleration-vs-time between  $t_i$  and  $t_f$  gives  $\Delta v_x$

$$v_{xf} = v_{xi} + \Delta v_x \leftarrow \text{Area under curve}$$

• Note about Notation: "your book uses the symbol 's' for a generic axis (it could be x-axis, y-axis, along an inclined plane,...)"

$$v_s = ds/dt \rightarrow v_x = dx/dt$$

$$\rightarrow v_y = dy/dt$$

**Motion with constant acceleration**

Uniform motion  $\rightarrow$  acceleration is zero  
(Object traveling at a constant speed)

$$v_{avg, x} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{\Delta t}$$

$$(x_f - x_i) = (v_{avg, x}) \Delta t \rightarrow x_f - x_i = v_x \Delta t \quad (v_x = \text{constant}, v_{avg, x})$$

**UNIFORM MOTION:**  $x_f = x_i + v_x \Delta t$   
OR  
 $y_f = y_i + v_y \Delta t$

$\rightarrow$  same thing as distance = speed  $\times$  time

Question: A car travels up a hill at a constant speed of 40 km/hr and returns down the hill at a constant speed of 60 km/hr. What is the avg. speed for the round trip?

less than 50 km/hr

length of hill = D

$$\text{avg. speed} = \frac{D + D}{t_{up} + t_{down}} = \frac{D + D}{\frac{D}{40 \text{ km/hr}} + \frac{D}{60 \text{ km/hr}}} \Rightarrow$$

need  $\Rightarrow$   $\frac{2D}{D \left( \frac{1}{40 \text{ km/hr}} + \frac{1}{60 \text{ km/hr}} \right)} = \underline{\underline{48 \text{ km/hr}}}$

CH2

February 5<sup>th</sup>, 2019

### Equations of constant acceleration.

↳ Set of equation that relate position, velocity & acceleration

\* Apply only if acceleration is constant in both magnitude & direction

$$v = \frac{dx}{dt}$$

$$\int_{t_i}^{t_f} v dt = \int_{t_i}^{t_f} \frac{dx}{dt} dt$$

\* v is a function of time so can't be taken out of integral

$$a = \frac{dv}{dt}$$

$$\int_{t_i}^{t_f} a dt = \int_{t_i}^{t_f} \frac{dv}{dt} dt$$

$$= a \int_{t_i}^{t_f} dt = a \Delta t \quad \text{" } v(t) \Big|_{t_i}^{t_f} = v_f - v_i$$

$$a \Delta t = v_f - v_i$$

$$v_f = v_i + a \Delta t$$

$$\rightarrow v_f = v_i + at$$

$$\int_{t_i}^{t_f} v(t) dt = \int_{t_i}^{t_f} \frac{dx}{dt} dt$$

February 7<sup>th</sup>, 2019

### Equations of Constant Acceleration.

↳ Relate initial & final positions, initial & final velocities, constant acceleration, & elapsed time

→ only apply if  $\vec{a}$  is constant in both magnitude & direction.

February 7, 2019

Variables used in book

Variables used in class

- $x_0$  initial position (position at the start of the time interval)
- $x$  final position (position at the end of the time interval)
- $v_{0x}$  initial velocity (velocity at the start of the time interval)
- $v_x$  final velocity (velocity at the end of the time interval  $\Delta t$ )
- $a_x$  Constant acceleration
- $t$  Elapsed time

Equations

$$v_x = v_{0x} + a_x t$$

$$x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$$

$$v_x^2 = v_{0x}^2 + 2 a_x (x - x_0)$$

$$x - x_0 = \frac{1}{2} (v_{0x} + v_x) t$$

Derivation

$$a_x = \frac{dv_x}{dt}$$

$$a_x dt = \frac{dv_x}{dt} \cdot dt \Rightarrow a_x \int_0^t dt = v_x(t) \Big|_0^t \Rightarrow a_x t \Big|_0^t = v_x(t) - v_x(0)$$

$$a_x t = v_x - v_{0x} \Rightarrow \underline{v_x = v_{0x} + a_x t}$$



Ch 2.

February 7, 2019

Part 2

$$x_0 = 125\text{m}$$

$$x = 0\text{m}$$

$$v_{0x} = 25\text{m/s}$$

$$v_x = 0\text{m/s}$$

$$a_x = -3.0\text{m/s}^2$$

$$t = ? \quad 8.33\text{s}$$

$=0$

$$v_x = v_{0x} + a_x t$$

$$0 = v_{0x} + a_x t$$

$$t = \frac{-v_{0x}}{a_x}$$

$$t = \frac{-25\text{m/s}}{-3.0\text{m/s}^2} = \underline{8.33\text{s}}$$

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$$

$$x = 125\text{m} + (25\text{m/s})(8.33\text{s}) + \frac{1}{2}(-3.0\frac{\text{m}}{\text{s}^2})(8.33\text{s})^2$$

$$\boxed{x = 229} \quad \text{Total distance traveled}$$

$$\text{Total Time: } 10\text{s} + 8.33\text{s} = \boxed{18\text{s}}$$

Ch 2. + RECAP

February 7, 2019

Part 2

$$x_0 = 125\text{m}$$

$$x = 0\text{m}$$

$$v_{0x} = 25\text{m/s}$$

$$v_x = 0\text{m}$$

$$a_x = -3.0\text{m/s}^2$$

$$t = ? \quad 8.33\text{s}$$

$$\stackrel{=0}{v_x} = v_{0x} + a_x t$$

$$0 = v_{0x} + a_x t$$

$$t = \frac{-v_{0x}}{a_x}$$

$$t = \frac{-25\text{m/s}}{-3.0\text{m/s}^2} = \underline{8.33\text{s}}$$

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$$

$$x = 125\text{m} + (25\text{m/s})(8.33\text{s}) + \frac{1}{2}(-3.0\frac{\text{m}}{\text{s}^2})(8.33\text{s})^2$$

$$x = \underline{229} \quad \text{Total distance traveled}$$

$$\text{Total Time: } 10\text{s} + 8.33\text{s} = \underline{18\text{s}}$$

RECAP

February 11, 2019

$x_0$	$v_x = v_{0x} + a_x t$
$x$	$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$
$v_{0x}$	$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$
$v_x$	$x - x_0 = \frac{1}{2}(v_{0x} + v_x)t$
$a_x$	
$t$	

### PROBLEM SOLVING STRATEGY

- 0) Read the problem & visualize
- 1) Draw a motion diagram (label  $\vec{v}$  and  $\vec{a}$ )
- 2) Make a table of known & unknown quantities
- 3) Solve algebraically for the unknown quantity  
(plug in zero first)

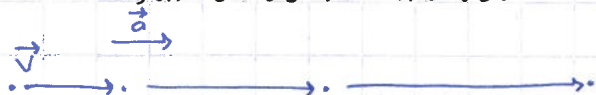
4) Plug in known values

5) Make sure your answers seems reasonable

EX

A car start from rest & accelerates at  $5.0 \text{ m/s}^2$  for  $10.0 \text{ s}$

How far does it travel?



$$x_0 = 0 \text{ m}$$

$$x = ? \text{ 250 m}$$

$$v_{0x} = 0 \text{ m/s}$$

$$v_x = 50 \text{ m/s}$$

$$a_x = 5.0 \text{ m/s}^2$$

$$t = 10.0 \text{ s}$$

$$v_x = v_{0x} + a_x t$$

$$v_x = a_x t$$

$$v_x = 5.0 \text{ m/s}^2 (10.0 \text{ s})$$

$$v_x = 50 \text{ m/s}$$

$$x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$$

$$x = \frac{1}{2} a_x t^2$$

$$x = \frac{1}{2} (5.0 \text{ m/s}^2) (10.0 \text{ s})^2$$

$$x = 250 \text{ m} \text{ OR } x = 2.5 \times 10^2 \text{ m}$$

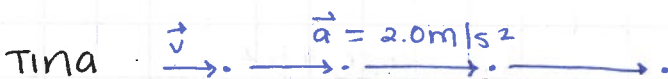
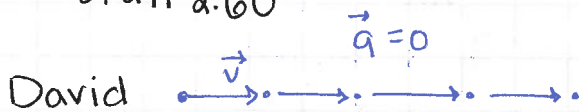
check:

$$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$$

$$v_x^2 = 2a_x(x)$$

$$x = \frac{v_x^2}{2a_x} \rightarrow x = \frac{(50 \text{ m/s})^2}{2(5.0 \text{ m/s}^2)} = 2.5 \times 10^2 \text{ m}$$

Problem 2.68



David

Tina

$$x_0 = 0 \text{ m}$$

$$x_0 = 0 \text{ m}$$

$$x = ?$$

$$x = ?$$

$$v_{0x} = 30 \text{ m/s}$$

$$v_{0x} = 0 \text{ m/s}$$

$$v_x = 30 \text{ m/s}$$

$$v_x = ?$$

$$a_x = 0 \text{ m/s}^2$$

$$a_x = 2.0 \text{ m/s}^2$$

$$t = ?$$

$$t = ?$$

a)  $x_{\text{David}} = x_{\text{Tina}}$

$$x_0 + v_{0x} t + \frac{1}{2} a_x t^2 = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$$

$$v_{0x} t = \frac{1}{2} a_x t^2$$

$$t = \frac{2v_{0x}}{a_x} \rightarrow t = \frac{2(30.0 \text{ m/s})}{2.0 \text{ m/s}^2} = 30.0 \text{ s}$$

→

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Continued...

$$x_{\text{David}} = (30.0 \text{ m/s})(30.0 \text{ s}) = \underline{900 \text{ m}}$$

$$x_{\text{Anna}} = \frac{1}{2}(2.0 \text{ m/s}^2)(30.0 \text{ s})^2 = \underline{900 \text{ m}}$$

$$v_x = v_{x0} + a_x t$$

$$v_x = a_x t$$

$$v_x = (2.0 \text{ m/s}^2)(30.0 \text{ s}) = \underline{60 \text{ m/s}}$$

**Free Fall** → (one-dimensional) motion

Where gravity is the only force acting on the object  
(NO air resistance)

\* In free fall, all objects accelerate at the same rate

$$a_y = -9.80 \text{ m/s}^2 = -g$$

$$g = 9.80 \text{ m/s}^2$$

\*  $g$  is always a + number; you will never use  $-9.80 \text{ m/s}^2$  for  $g$ .

acceleration due to gravity =  $9.80 \text{ m/s}^2$  straight downward  
=  $-9.80 \text{ m/s}^2$   
=  $-g$

Equations for Free Fall:

$$v_y = v_{y0} + a_y t$$

$$y = y_0 + v_{y0} t + \frac{1}{2} a_y t^2$$

$$v_y^2 = v_{y0}^2 + 2a_y (y - y_0)$$

$$y - y_0 = \frac{1}{2} (v_{y0} + v_y) t$$

$$a_y = -9.80 \text{ m/s}^2$$

( $9.80 \text{ m/s}^2$  straight downward)

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ex A ball is thrown straight upwards at  $30.0 \text{ m/s}$   $v_y = 0 \text{ m/s}$

a) How long does it take to reach the highest point?

b) How long is it in the air for? (Assuming it is caught at the same height it is released from?)

a)  $y_0 = 0 \text{ m}$

$y = ?$

$v_{0y} = 30.0 \text{ m/s}$

$v_y = 0 \text{ m/s}$  at highest point

$a_y = -9.80 \text{ m/s}^2$

$t = ? \rightarrow 3.1 \text{ s}$  (to highest point)

$v_y = 0$   
 $v_y = v_{0y} + a_y t$

$0 = v_{0y} + a_y t$

$t = \frac{-v_{0y}}{a_y} = \frac{-30.0 \text{ m/s}}{-9.80 \text{ m/s}^2} \Rightarrow \underline{t = 3.1 \text{ s}}$

b)  $y_0 = 0 \text{ m}$

$y = 0 \text{ m}$

$v_{0y} = 30.0 \text{ m/s}$

$v_y = ?$

$a_y = -9.80 \text{ m/s}^2$

$t = ?$   $6.2 \text{ s}$

$y = y_0 = v_{0y} t + \frac{1}{2} a_y t^2$

$0 = v_{0y} t + \frac{1}{2} a_y t^2$

$-v_{0y} t = \frac{1}{2} a_y t^2$

$t = \frac{-2 v_{0y}}{a_y}$

$t = \frac{-2(30.0 \text{ m/s})}{-9.80 \text{ m/s}^2} = \underline{6.2 \text{ s}}$

Free Fall

\* At the highest point,  $v_y = 0 \text{ m/s}^2$  ( $a_y = -9.80 \text{ m/s}^2$ )

\* Time up = time down (assuming  $y = y_0$ )

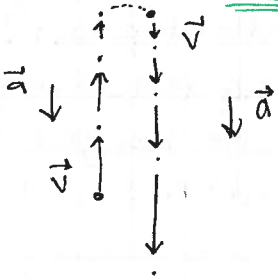
(time in air = 2x time to highest point)

\* Free Fall motion is symmetric - at a given height, Speed is the same (velocities are opp.)

Ch2 + Recap

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Problem 2.21



$y_0 = 2.0\text{m}$

$y = 0\text{m}$

$v_{0y} = 15\text{m/s}$

$v_y = ?$

$a_y = -9.80\text{m/s}^2$

$t = ?$

$t = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$

$A = 1/2 a_y = -4.90\text{m/s}^2$

$B = v_{0y} = 15.0\text{m/s}$

$C = y_0 = 2.0\text{m}$

$t = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$

$t = \frac{-15.0\text{m/s} \pm \sqrt{(15.0\text{m/s})^2 - 4(-4.90\text{m/s}^2)(2.0\text{m})}}{2(-4.90\text{m/s}^2)}$

$y = y_0 + v_{0y}t + 1/2 a_y t^2$

$1/2 a_y t^2 + v_{0y}t + y_0 = 0$   
 $(Ax^2 + Bx + C = 0)$

$t = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$

$t = 3.2\text{s}$   
 and  
 $t = \text{neg \#}$

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RECAP

Equations of constant acceleration:

$v_x = v_{0x} + a_x t$

$x = x_0 + v_{0x}t + 1/2 a_x t^2$

$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$

$x - x_0 = 1/2 (v_{0x} + v_x)t$

Horizontal motion or  
motion along an inclined plane  
 ↳ today

Free Fall → Gravity is the only force acting

$v_y = v_{0y} + a_y t$

$y = y_0 + v_{0y}t + 1/2 a_y t^2$

$v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$

$y - y_0 = 1/2 (v_{0y} + v_y)t$

Vertical motion on  
 free fall

ONLY in  
 Free fall

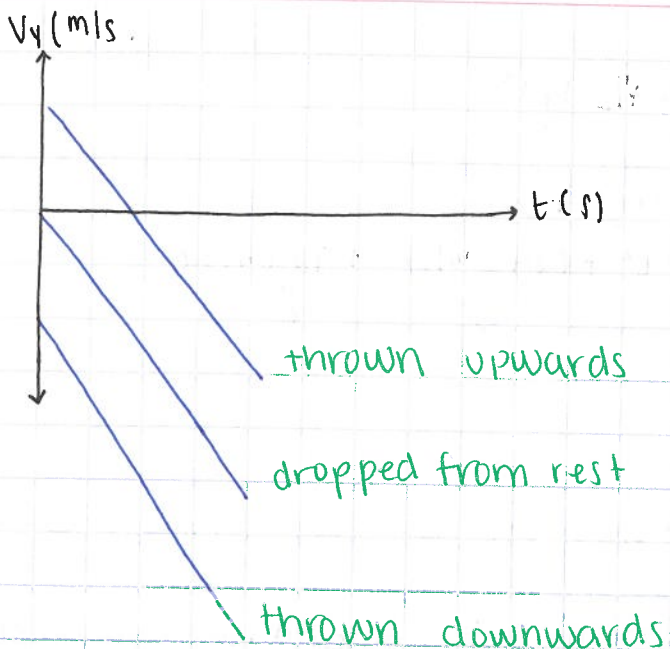
$a_y = -g = -9.80\text{m/s}^2$

$a = -9.80\text{m/s}^2$  →  
 (time in air = 2x time  
 to highest point)

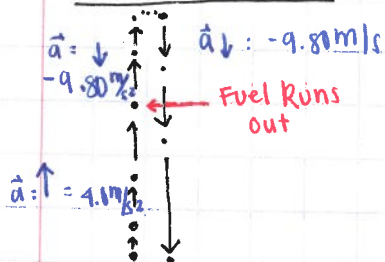
- \*  $v_y = 0\text{m/s}$  at highest point
- \* time up = time down if  $y = y_0$
- \* Motion is symmetric

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PROBLEM 2.C



Part 1 →  $a = 4.00 \text{ m/s}^2$

- $y_0 = 6 \text{ m}$
- $y = ?$
- $v_{0y} = 0 \text{ m/s}$
- $v_y = ?$
- $a_y = 4.00 \text{ m/s}^2$
- $t = 6.0 \text{ s}$

$$v_y = v_{0y} + a_y t$$

$$v_y = a_y t$$

$$v_y = (+4.00 \text{ m/s}^2)(6.00 \text{ s})$$

$$v_y = \underline{24.0 \text{ m/s}}$$

$$y - y_0 = \frac{1}{2} (v_{0y} + v_y) t$$

$$y = \frac{1}{2} (+24 \text{ m/s}) t$$

$$y = \frac{1}{2} (+24 \text{ m/s})(6.00 \text{ s})$$

$$y = \underline{72.0 \text{ m}}$$

PART 2

- $y_0 = 72 \text{ m}$
- $y = ?$
- $v_{0y} = +24 \text{ m/s}$
- $v_y = 0 \text{ m/s}$
- $a_y = -9.80 \text{ m/s}^2$
- $t = ?$

$$v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$$

$$0 = v_{0y}^2 + 2a_y(y - y_0)$$

$$y - y_0 = -\frac{v_{0y}^2}{2a_y}$$

$$y = y_0 - \frac{v_{0y}^2}{2a_y} \rightarrow y = 72 \text{ m} - \frac{(24 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)}$$

$y = \underline{101 \text{ m}}$

2.

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2C

$$y = y_0 + v_{0y}t + \frac{1}{2}a_y t^2$$

$$\frac{1}{2}a_y t^2 + v_{0y}t + y_0 = 0$$

$$-4.90 \text{ m/s}^2 t^2 + (24.0 \text{ m/s})t + 72.0 \text{ m} = 0$$

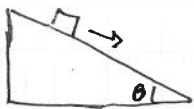
$$t = 7.0 \text{ s}$$

$$t_{\text{re}} = 6.0 \text{ s} + 7.0 \text{ s} = 13.0 \text{ s}$$

is released from a balloon that is descending at a constant of 10 m/s....

$y + a_y t$   
 $10 \text{ m/s} + (-9.80 \text{ m/s}^2)(20.0 \text{ s})$   
 $206 \text{ m/s}$   
 is 206 in the neg. direction.

**ALONG A frictionless Inclined Plane**



\*acceleration on a frictionless inclined plane is

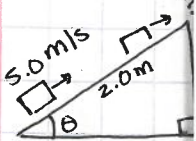
$$a_x = g \sin \theta \text{ down the plane}$$

$$a_x = (9.80 \text{ m/s}^2) \sin 0^\circ = 0 \text{ m/s}^2$$

$$a_x = (9.80 \text{ m/s}^2) \sin 90^\circ = 9.80 \text{ m/s}^2$$

ch. 2.

PROBLEM



$$x_0 = 0 \text{ m}$$

$$x = 2.0 \text{ m}$$

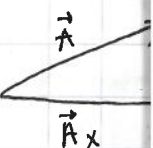
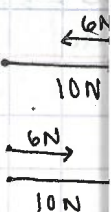
$$v_{0x} = 5.0 \text{ m/s}$$

$$v_x = ?$$

$$a_x = -4.9 \text{ m/s}^2$$

$$t = ?$$

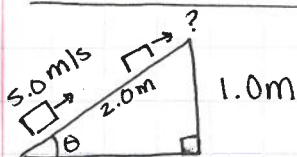
Chapter



Vector →

ch. 2. & Ch. 3: Vectors & Coord. Systems. February 12, 2019

PROBLEM 2.30



$$\theta = \sin^{-1} \left( \frac{1.0 \text{ m}}{2.0 \text{ m}} \right) = 30^\circ$$

$$a_x = g \sin \theta = 9.80 \text{ m/s}^2 \left( \frac{1.0 \text{ m}}{2.0 \text{ m}} \right) = 4.90 \text{ m/s}^2 \leftarrow \text{down the incline}$$

$x_0: 0 \text{ m}$

$x: 2.0 \text{ m}$

$v_{0x}: 5.0 \text{ m/s}$

$v_x: ?$

$a_x: -4.90 \text{ m/s}^2$

$t: ?$

$$v_x^2 = v_{0x}^2 + 2a_x(x - x_0) \quad \text{---} = 0$$

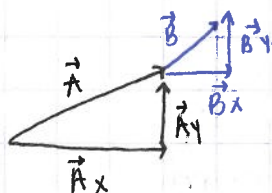
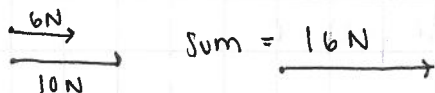
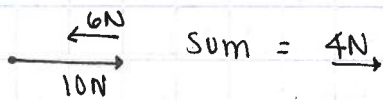
$$v_x^2 = v_{0x}^2 + 2a_x(x)$$

$$v_x = \pm \sqrt{v_{0x}^2 + 2a_x(x)}$$

$$v_x = \sqrt{(5.0 \text{ m/s})^2 + 2(-4.90 \text{ m/s}^2)(2.0 \text{ m})}$$

$$v_x = 2.3 \text{ m/s}$$

Chapter 3: Vectors & Coordinate Systems



Sum  $\vec{C}$

$$C_x = A_x + B_x$$

$$C_y = A_y + B_y$$

February 14, 2019

Vector  $\rightarrow$  physical quantity with both magnitude and a direction

$\hookrightarrow$  indicates direction in one-dimension

numbers + units